



Friday 20 January 2012 – Afternoon

AS GCE MATHEMATICS

4725 Further Pure Mathematics 1

QUESTION PAPER

Candidates answer on the Printed Answer Book.

OCR supplied materials:

- Printed Answer Book 4725
- List of Formulae (MF1)

Other materials required:

· Scientific or graphical calculator

Duration: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found in the centre of the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- Write your answer to each question in the space provided in the Printed Answer Book. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer all the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.

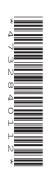
INFORMATION FOR CANDIDATES

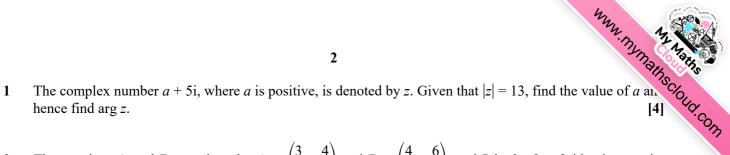
This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [] at the end of each question or part question on the Question Paper.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is 72.
- The Printed Answer Book consists of **12** pages. The Question Paper consists of **4** pages. Any blank pages are indicated.

INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

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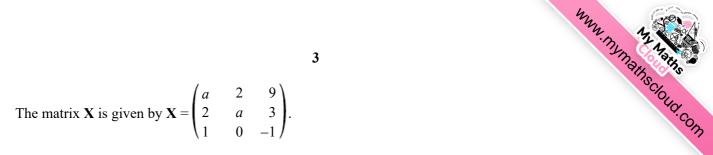


- The matrices **A** and **B** are given by $\mathbf{A} = \begin{pmatrix} 3 & 4 \\ 2 & -3 \end{pmatrix}$ and $\mathbf{B} = \begin{pmatrix} 4 & 6 \\ 3 & -5 \end{pmatrix}$, and **I** is the 2 × 2 identity matrix. 2 Given that $p\mathbf{A} + q\mathbf{B} = \mathbf{I}$, find the values of the constants p and q. [5]
- 3 Use an algebraic method to find the square roots of $3 + (6\sqrt{2})i$. Give your answers in the form x + iy, where x and y are exact real numbers.
- Find $\sum_{n=1}^{n} r(r^2 3)$, expressing your answer in a fully factorised form. 4 [6]
- 5 (a) Find the matrix that represents a reflection in the line y = -x. [2]
 - **(b)** The matrix **C** is given by $\mathbf{C} = \begin{pmatrix} 1 & 0 \\ 0 & 4 \end{pmatrix}$.
 - (i) Describe fully the geometrical transformation represented by C. [2]
 - (ii) State the value of the determinant of C and describe briefly how this value relates to the transformation represented by C. [2]
- Sketch, on a single Argand diagram, the loci given by $|z \sqrt{3} i| = 2$ and $\arg z = \frac{1}{6}\pi$. 6 [6]
- The matrix **M** is given by $\mathbf{M} = \begin{pmatrix} 3 & 0 \\ 2 & 1 \end{pmatrix}$. 7
 - (i) Show that $\mathbf{M}^4 = \begin{pmatrix} 81 & 0 \\ 80 & 1 \end{pmatrix}$. [3]
 - (ii) Hence suggest a suitable form for the matrix \mathbf{M}^n , where n is a positive integer. [2]
 - (iii) Use induction to prove that your answer to part (ii) is correct. [4]
- (i) Show that $\frac{r}{r+1} \frac{r-1}{r} = \frac{1}{r(r+1)}$. 8 [2]
 - (ii) Hence find an expression, in terms of n, for

$$\frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \dots + \frac{1}{n(n+1)}$$
 [4]

(iii) Hence find
$$\sum_{r=n+1}^{\infty} \frac{1}{r(r+1)}$$
. [2]

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- (i) Find the determinant of X in terms of a. [3]
- (ii) Hence find the values of a for which X is singular. [3]
- (iii) Given that X is non-singular, find X^{-1} in terms of a. [4]
- The cubic equation $3x^3 9x^2 + 6x + 2 = 0$ has roots α , β and γ . 10

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(i) Write down the values of $\alpha + \beta + \gamma$, $\alpha\beta + \beta\gamma + \gamma\alpha$ and $\alpha\beta\gamma$. [3]

The cubic equation $x^3 + ax^2 + bx + c = 0$ has roots α^2 , β^2 and γ^2 .

(ii) Show that
$$c = -\frac{4}{9}$$
 and find the values of a and b. [9]

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